

Noise and information in Econophysics

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Outline

- A few concepts in finance
- Aggregation and filtering of information in complex systems
- Random matrix theory and proximity based networks
- Trading decisions in the presence of exhogenous and endogenous market signals
- Conclusions

Econophysics is a hybrid discipline



Financial markets

A financial market can be considered as a 'model' complex system.





In a financial market there are many heterogeneous agents interacting to perform the collective task of finding the best price for financial assets.



Market efficiency definition

"A capital market is said to be efficient if it fully and correctly reflects all relevant information in determining security prices. Formally, the market is said to be efficient with respect to some information set if security prices would be unaffected by revealing that information to all participants. Moreover, efficiency with respect to an information set implies that it is impossible to make economic profits by trading on the basis of that information set"[¶]

[¶] B. Malkiel, Efficient market hypothesis, New Palgrave Dictionary of Money and Finance, Macmillan, London 1992

Information aggregation in markets

The first observation that markets can act as institutions performing information aggregation is due to Fredrich van Hayek. In his 1945 work on "The use of knowledge in society" he wrote:

"The mere fact that there is one price for any commodity – or rather that local prices are connected in a manner determined by the cost of transport, etc. – brings about the solution which (it is just conceptually possible) might have been arrived at by one single mind possessing all the information which is in fact dispersed among all the people involved in the process."

Hayek FA. The Use of Knowledge in Society. American Economic Review. 1945;35(4):519-30.

Arbitrage opportunity

One of the main paradigms used for the modeling of price dynamics in a financial market is the concept of absence of **arbitrage opportunity**.

An *arbitrage opportunity* is present in a market when an economic actor can devise a trading strategy which is able to provide her or him a financial gain continuously and without risk.

An example



At a given time 1 kg of wheat costs 1.30 USD in St. Louis and 1.45 USD in Miami.

The cost of transporting and storing 1 kg of wheat from St. Louis to Miami is 0.05 USD

By buying 10,000 kg in St. Louis and selling them immediately after in Miami it is possible to make a risk-free profit

10000 (1.45-1.30-0.05)=1000 USD

Exploited arbitrage opportunities

If this action is repeated this implies that the demand of wheat (and therefore its price) in St. Louis increases whereas the supply in Miami increases and its price decreases.

In an efficient market, the exploiting of an arbitrage opportunity implies its disappearance in a (usually) short time period.

The absence of arbitrage opportunity implies that the price of a financial asset is hard to predict or **unpredictable**.

Geometric Brownian motion

In 1965, Paul Samuelson[‡] formalized the assumption that properly anticipated stock prices should behave as random processes.

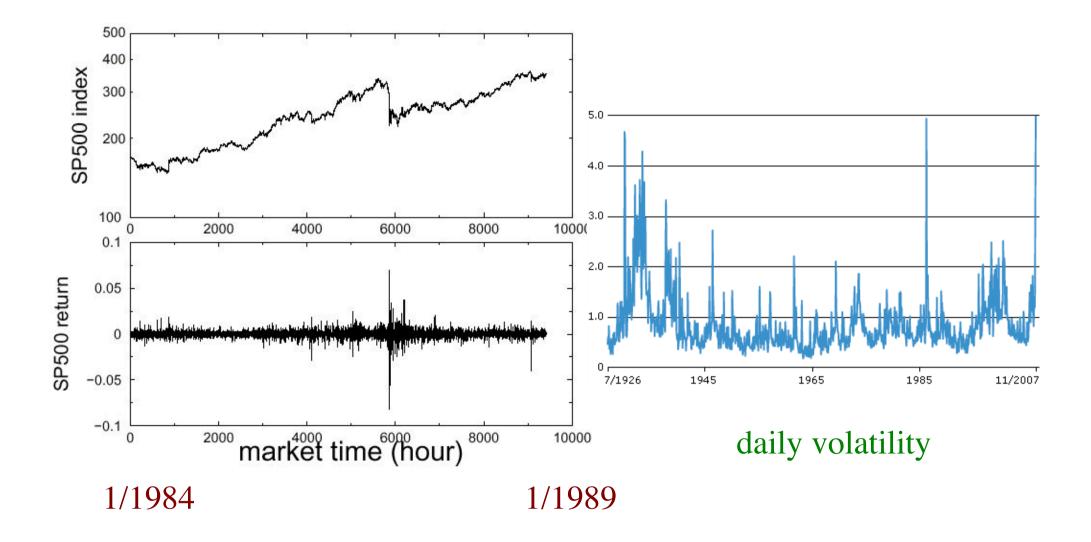
The geometric Brownian motion is considered the simplest random process describing the price dynamics of a financial asset.

 $dP(t) = \mu P(t)dt + \sigma P(t)dW$

An idealized model of stock market where the stock price dynamics is described by a geometric Brownian motion exists and provides the theoretical foundation for quantitative finance.

[‡]P. Samuelson, Industrial Man. Review, **6**, 41-45 (1965)

The price (and return) dynamics of a financial asset



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The Prize in Economic Sciences 2013





Eugene F. Fama University of Chicago, IL, USA



Lars Peter Hansen University of Chicago, IL, USA

"för deras empiriska analys av tillgångspriser"



Robert J. Shiller Yale University, New Haven, CT, USA

The Nobel committee is muddled on the nature of economics



By John Kay

The term 'rationality' lacks relevance in a world characterised by imperfect information

The Royal Swedish Academy of Sciences continues to astonish the public when awarding the Nobel Memorial Prize in Economics. In 2011 it celebrated the success of recent research in promoting macroeconomic stability. This year it pays tribute to the capacity of economists to predict the long-run movement of asset prices.

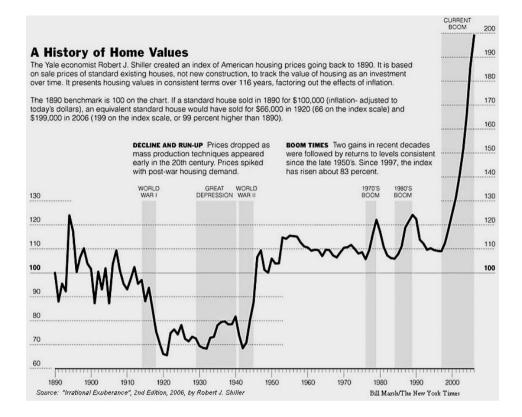
People with knowledge of financial economics may be further surprised that this year Eugene Fama and Robert Shiller are both recipients. Prof Fama made his name by developing the efficient market hypothesis, long the cornerstone of finance theory. Prof Shiller is the most prominent critic of that hypothesis. It is like awarding the physics prize jointly to Ptolemy for his theory that the Earth is the centre of the universe, and to Copernicus for showing it is not.

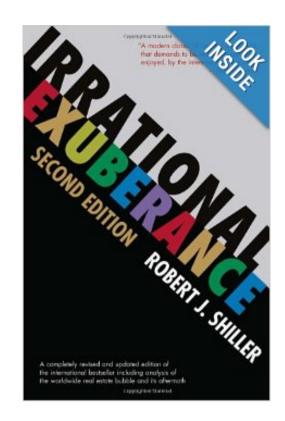
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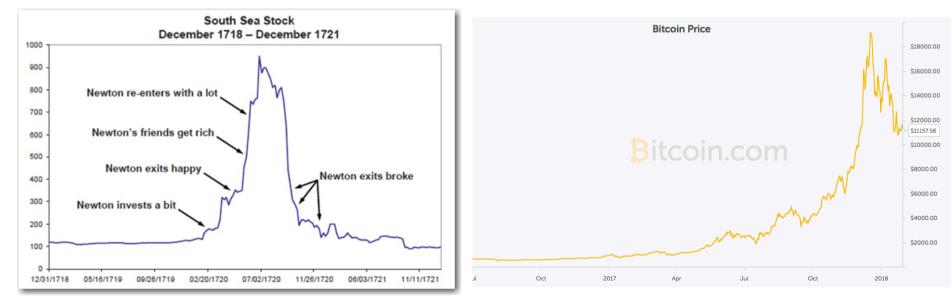
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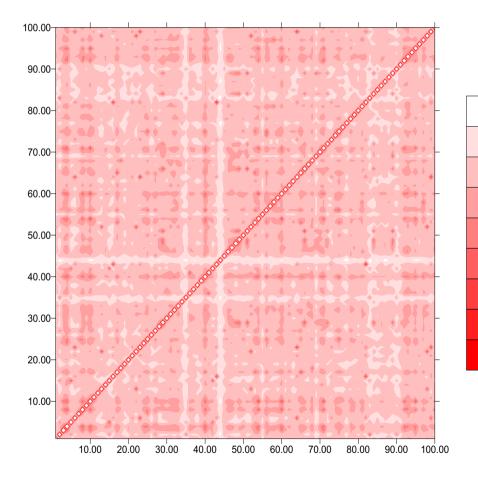


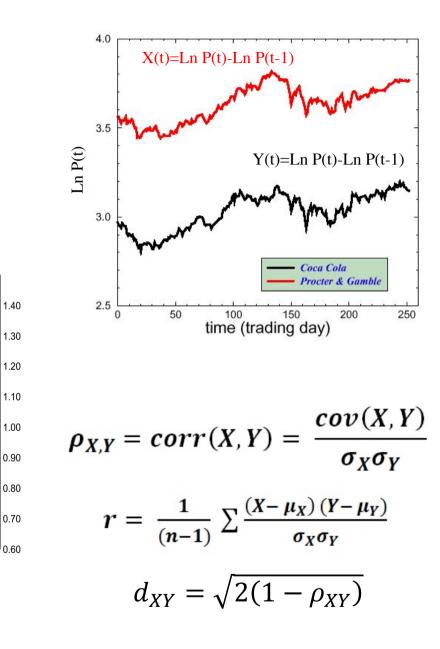




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Information is present in the multivariate time evolution of asset returns





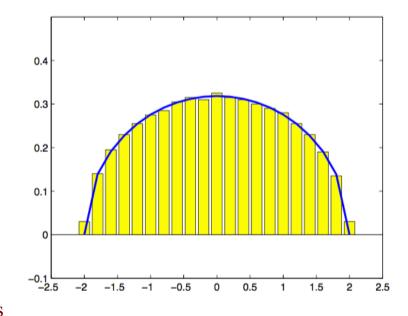
The Semi-circle law in Random Matrix Theory

In 1955, Wigner showed that the limiting eigenvalue distribution of random symmetric $n \times n$ matrices $X = (A + A^T)/2$ where A = G(n, n),

follows a semi-circle distribution, which is given by

$$\rho\left(\tilde{\lambda}\right) = \frac{1}{2\pi}\sqrt{4-\tilde{\lambda}^2}$$

When properly normalized $\tilde{\lambda} = \lambda / \sqrt{n/2}$, the curve looks like a semi-circle of radius 2



E. P. Wigner. Characteristic vectors of bordered matrices with infinite dimensions. Annals of Mathematics, 62:548–564, 1955.

Semi-circle law with one 1000 \times 1000 matrix.

Random Matrix Theory for correlation of random Gaussian variables

Suppose that N elements are described by T records, i.e. we have a random matrix with NxT records. Each record is a realization of independent Gaussian random variables with zero mean and variance σ^2 .

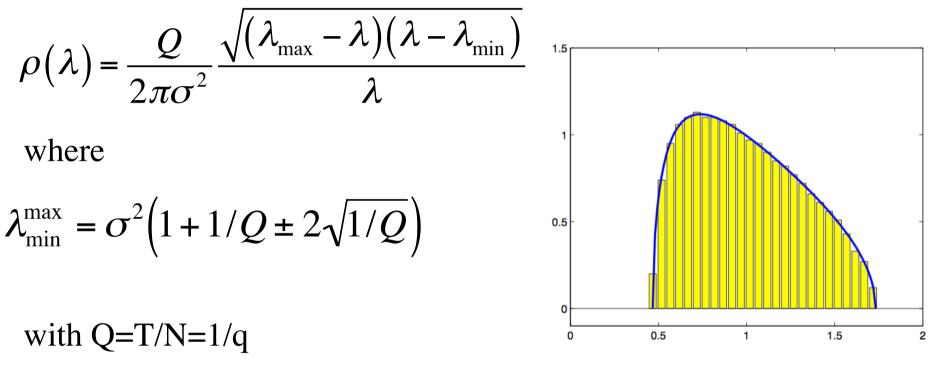
In the limit T -> ∞ , the correlation matrix of this set of N variables is the identity matrix, which has associated a spectrum of eigenvalues which is composed of N delta functions at $\lambda=1$

In the limit T, N -> ∞ with a fixed ratio Q=T/N \ge 1 random matrix theory provides the asymptotic probability density of the eigenvalues.

The convergence to the asymptotic pdf is already observed for relatively low values of N and T.

The asymptotic PDF of eigenvalues

The asymptotic probability density function is

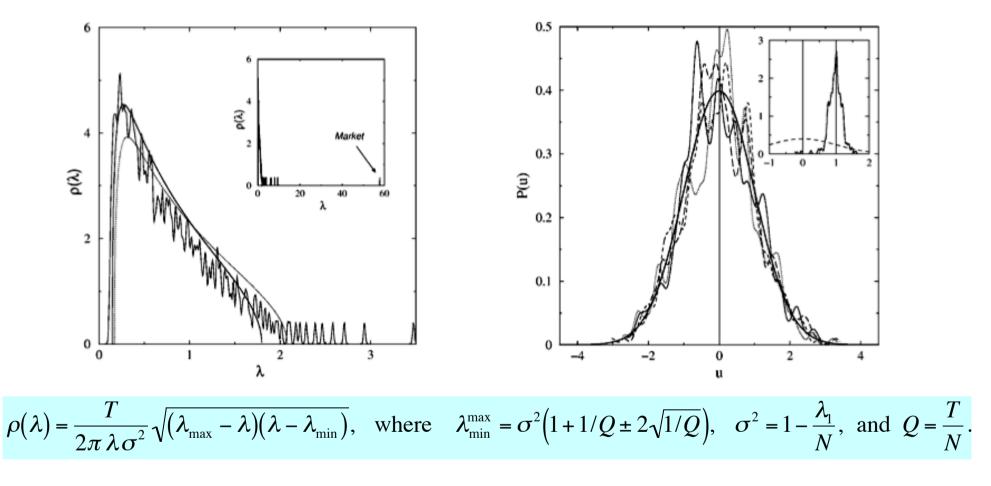


Marcenko-Pastur Law(q=0.1) with a NxT 2000 \times 20000 matrix X.

Marčenko, V.A. and Pastur, L.A., 1967. Distribution of eigenvalues for some sets of random matrices. Mathematics of the USSR-Sbornik, 1(4), p.457.

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Random Matrix Theory of financial correlation



L. Laloux, P. Cizeau, J.-P. Bouchaud & M. Potters, *Phys. Rev. Lett.* **83**, 1468 (1999). V. Plerou, P. Gopikrishnan, B. Rosenow, L. A. N. Amaral, and H. E. Stanley, *Phys. Rev. Lett.* **83**, 1471 (1999).

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Characteristics of the eigenvalue spectrum

The spectrum of a typical portfolio of financial assets (e.g. stocks) can be divided in three classes of eigenvalues:

 The largest eigenvalue describes the common behavior of stocks (what is called "the market").
It is incompatible with the random matrix theory of random variables.

2) A fraction of 5% of the eigenvalues is also incompatible with the random matrix theory because eigenvalues fall outside] λ_{min} , λ_{max} [

The low part of the spectrum

3) The remaining eigenvalues assume values between λ_{min} , λ_{max} and therefore one cannot say whether the eigenspace, which is corresponding to these eigenvalues, contains information or not.

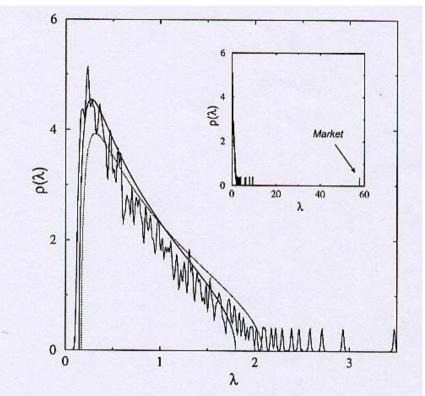
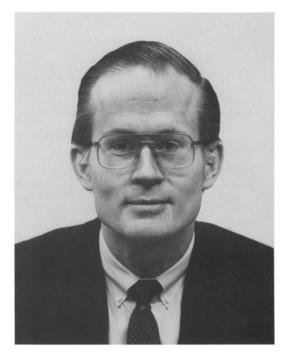


FIG. 1. Smoothed density of the eigenvalues of C, where the correlation matrix C is extracted from N = 406 assets of the S&P 500 during the years 1991–1996. For comparison we have plotted the density Eq. (3) for Q = 3.22 and $\sigma^2 = 0.85$: this is the theoretical value obtained assuming that the matrix is purely random except for its highest eigenvalue (dotted line). A better fit can be obtained with a smaller value of $\sigma^2 = 0.74$ (solid line), corresponding to 74% of the total variance. Inset: Same plot, but including the highest eigenvalue corresponding to the market, which is found to be 25 times greater than λ_{max} .



THE JOURNAL OF FINANCE • VOL. XLI, NO. 3 • JULY 1986

Noise

FISCHER BLACK*

ABSTRACT

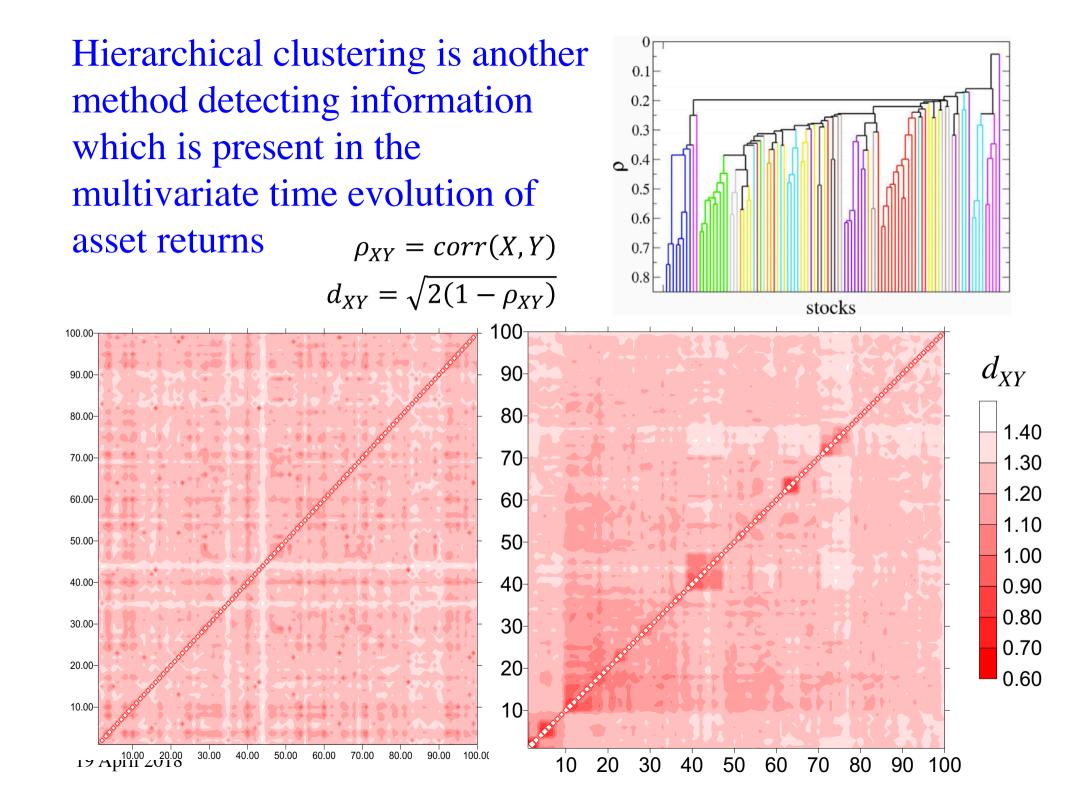
The effects of noise on the world, and on our views of the world, are profound. Noise in the sense of a large number of small events is often a causal factor much more powerful than a small number of large events can be. Noise makes trading in financial markets possible, and thus allows us to observe prices for financial assets. Noise causes markets to be somewhat inefficient, but often prevents us from taking advantage of inefficiencies. Noise in the form of uncertainty about future tastes and technology by sector causes business cycles, and makes them highly resistant to improvement through government intervention. Noise in the form of expectations that need not follow rational rules causes inflation to be what it is, at least in the absence of a gold standard or fixed exchange rates. Noise in the form of uncertainty about what relative prices would be with other exchange rates makes us think incorrectly that changes in exchange rates or inflation rates cause changes in trade or investment flows or economic activity. Most generally, noise makes it very difficult to test either practical or academic theories about the way that financial or economic markets work. We are forced to act largely in the dark.

In system where information is densely packed into sets of records (e.g. time series) we have noise and information simultaneously present.

When information is providing marginal advantage the discrimination between noise and information is not straightforward (all easy detections have been ruled out by the action of arbitrage opportunities).

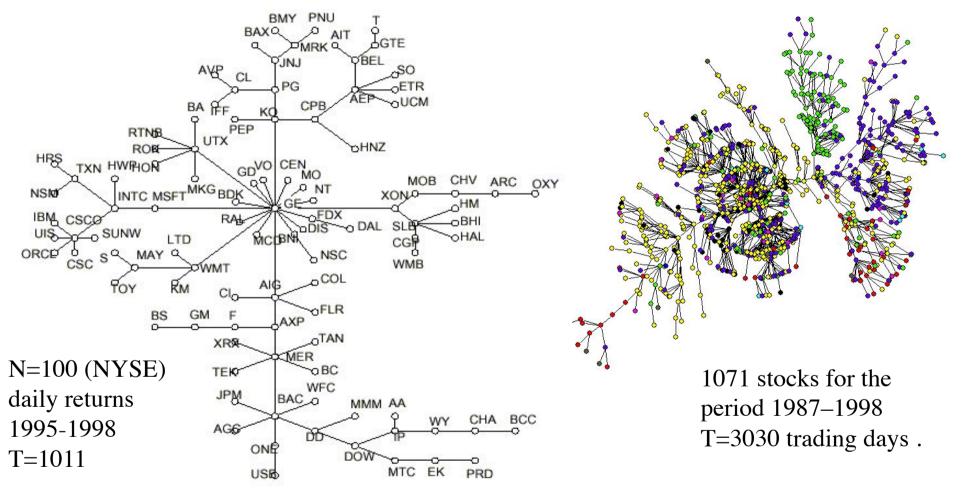
Random matrix theory suggests that some information is quite distinct from noise but there is also information hardly distinguishable from noise and noise hardly distinguishable from information.

Bouchaud and collaborators have coined the sentence that the correlation matrix is "noise dressed". My view is that some information is "dressed" as "noise" it is, i.e. it is hardly distinguishable from noise.



Another popular method of information filtering

Proximity based networks: Minimum spanning tree



Mantegna, R.N., 1999. Hierarchical structure in financial markets. The European Physical Journal B-11(1), pp.193-197.

Bonanno, G., Caldarelli, G., Lillo, F. and Mantegna, R.N., 2003. Topology of correlation-based minimal spanning trees in real and model markets. Physical Review E, 68(4), p.046130. 19 April 2018 University of Pavia 26

A data driven study: The NCSD database.

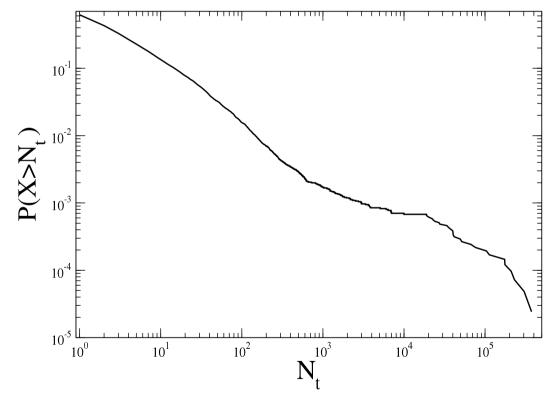
From January 1st, 1995 the Nordic Center Securities Data (NCSD) (today Euroclear) collects a database recording the daily ownership of financial portfolios and trading records (until 2009) of different categories of Finnish investors (companies, governmental investors, foreign institutions investors, non profit organizations, financial institutions and households).

Identity of the investors is coded for privacy reasons.

This database has been extensively investigated at the aggregated level of categories of investors in the financial literature by Grinblatt and Keloharju (2000, 2001,2009).

The set of investors is quite heterogeneous in terms of volume, frequency of trading, portfolio nature, wealth, etc.

Ex: Cumulative probability density $P(X > N_t)$ of the number of transactions N_t performed by 41250 Finnish legal entities trading the Nokia stock (typically but not exclusively at the Nordic Stock Exchange) during 2003.



The flux of financial news about Nokia: a proxy from **Thomson Reuters** Contact Us THOMSON REUTERS Search Q PRODUCTS & SERVICES ~ NEWS & IDEAS \sim HOME INVESTOR RELATIONS \sim ABOUT US \sim CAREERS FINANCIAL HOME > FINANCIAL PRODUCTS & SERVICES > PRODUCTS A-Z > Thomson Reuters NewsScope Application License PRODUCTS A-Z FINANCIAL FINANCIAL PRODUCTS & THOMSON REUTERS NEWSSCOPE APPLICATION LICENSE SERVICES Commodities Trading professionals trust Reuters news for its speed and accuracy. Now you can leverage the power of our global news to fuel your mission-critical applications and algorithms in real-time. Seize opportunities, exploit market inefficiencies and **Corporate Services** manage event risk with world-renowned news from Reuters. Deal Making Equities & Derivatives

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The set comprises 11 484 unique headlines.

2003-01-

10,12:48:07.604,"20030110124749nL1011908","**HEADLINE**","nL1011 908","2003-01-10 12:47:49","2003-01-10 12:48:07","**Finnish HEX**,

Nokia edge up on back of German data"," HELSINKI, Jan 10 (Reuters)

- Finnish stocks turned north at midsession on Friday with Nokia<NOK1V.HE> erasing earlier losses.

Nokia <NOK1V.HE>, the world's largest mobile phone maker and Forestries were followed Nokia in the top three traded reporting season that kicks off with Nokia on January 23.

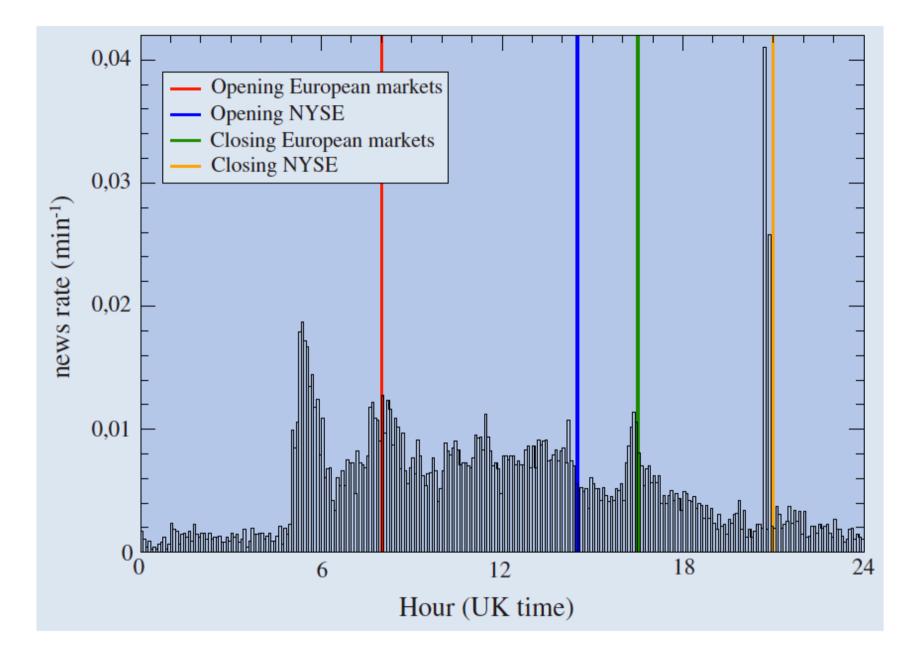


Figure 1. Average daily pattern of the arrival rate of news on the Nokia company. The rate is measured in number of headlines per minute. The vertical lines indicate the time of opening and closing of European and New York Stock Exchange market. Data are adjusted for the daylight saving time.

We consider the trading decisions of single investors trading Nokia stocks from Jan 2nd 2003 to Dec 30th 2008.

Category	# ids	N	V
Companies	8,396	1,009,226	4,825
Financial	392	$4,\!079,\!174$	$21,\!402$
Governamental	124	39,278	$1,\!985$
Non profit	922	21,778	248
Households	129,952	$1,\!555,\!096$	1,993
Foreign	1,405	789,552	$7,\!685$
Total	141,190	7,494,104	38,138

We define three categorical variables classifying the trading action of the investors. They are:

$$\frac{V_B - V_S}{V_B + V_S} > + \vartheta \qquad \text{Buy state}$$

Sell state

$$-\vartheta < \frac{V_B - V_S}{V_B + V_S} < +\vartheta$$
 with $V_B > 0$ and $V_S > 0$ **BuySell state**

with $\vartheta = 0.25$ and $\vartheta = 0.01$

Variables investigated

$$N^{K}(t) = N^{K}_{B}(t) + N^{K}_{S}(t) + N^{K}_{BS}(t)$$
$$\Delta N^{K}_{A}(t) = N^{K}_{B}(t) - N^{K}_{S}(t)$$
$$\Delta N^{K}_{R}(t) = \frac{N^{K}_{B}(t) - N^{K}_{S}}{N^{K}(t)}$$

Variables about market trading activity

$$Ret(t) = \log P(t) - \log P(t-1)$$
$$Vol(t) = 2\frac{P_{max}(t) - P_{min}(t)}{P_{max}(t) + P_{min}(t)}$$

Price dynamics market indicators

H(t)= # of headlines of news about Nokia

Variables about news

We also perform sentiment analysis on the text of the headlines (also stories have been analyzed).

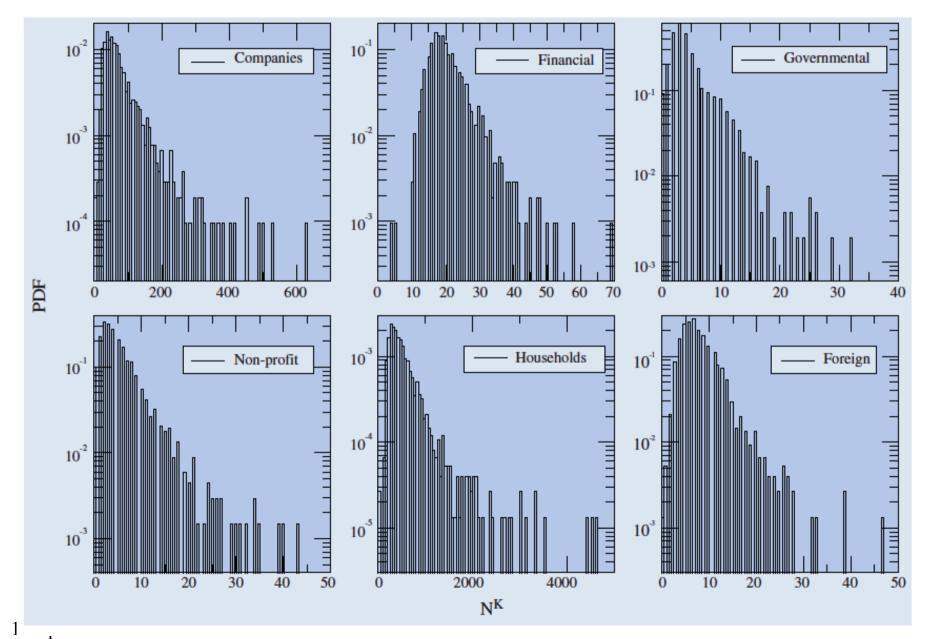
The sentiment analysis was performed by using General Inquire categories from the Harvard psychosocial dictionary

http://www.wjh.harvard.edu/~inquirer/

$$S_A(t) = G(t) - B(t)$$

$$S_R(t) = \frac{G(t) - B(t)}{G(t) + B(t)}$$

The tail of the probability density function of market activity N^K is approximately exponential for all categories of investors.



The basic explanatory variables are correlated

```
Corr[H, Vol]=0.501
```

```
Corr[S_A, Ret]=0.155
```

 $Corr[S_R, Ret]=0.118$

We therefore also consider the partial correlation among variables $\rho(x, y|z)$

between variables x and y conditioned on the variable z. This quantity is the Pearson correlation coefficient between the residuals of x and y that are uncorrelated with z.

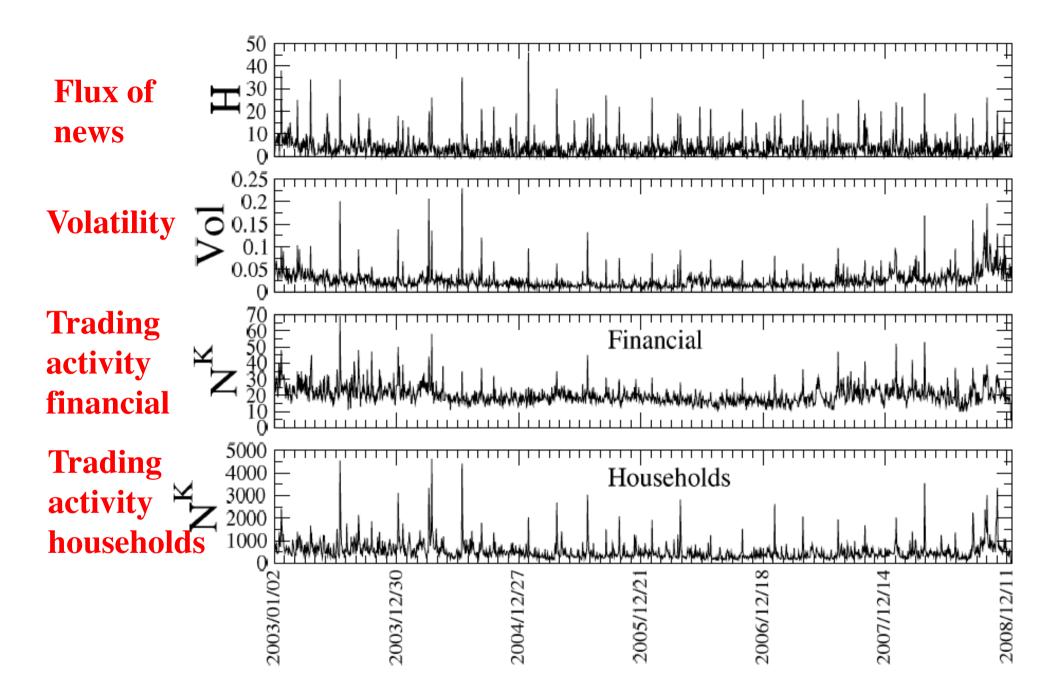
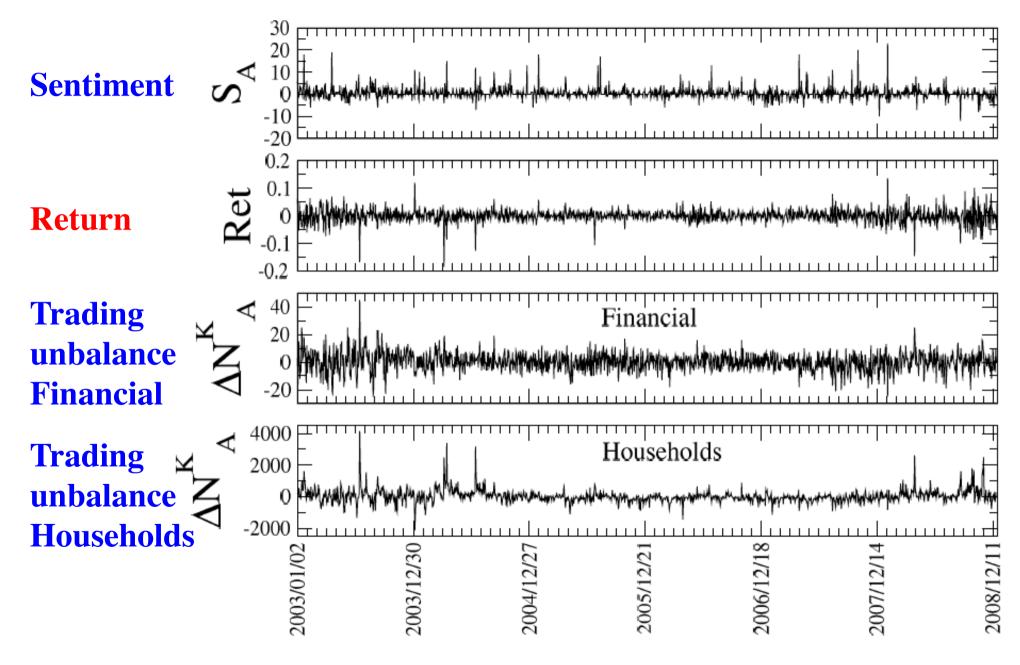
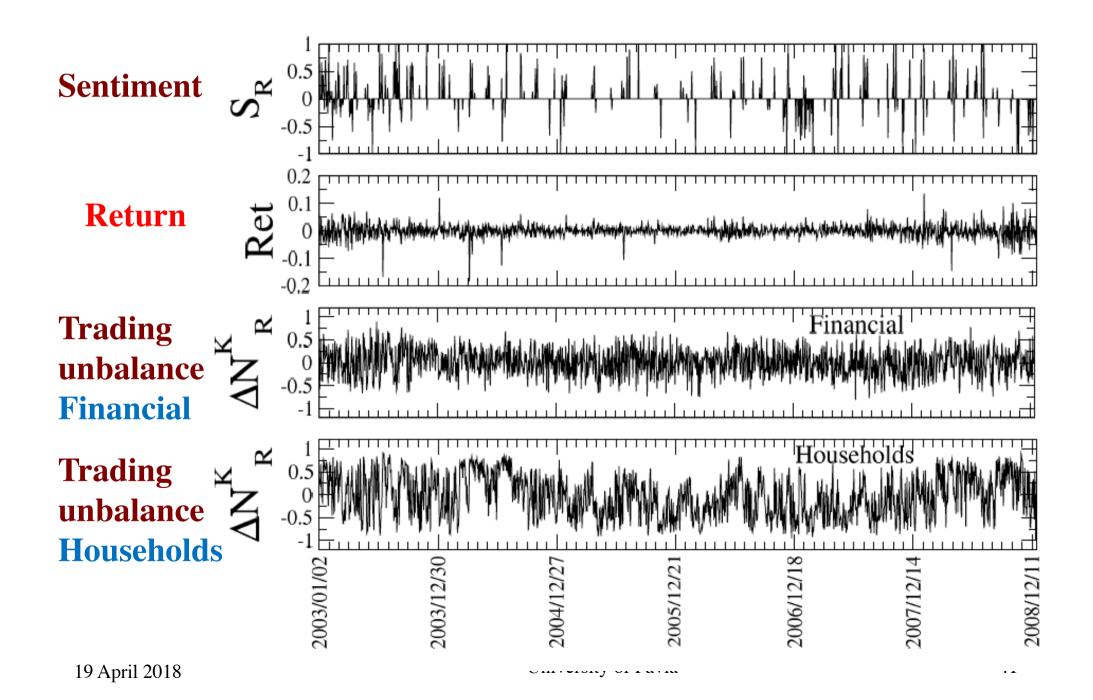


Figure 2. From top to bottom the figure shows the time series of the number of Nokia headlines H(t), the daily volatility Vol(t) of Nokia stock, and the time series of $N^{K}(t)$ for the category of Financial investors and for the category of Households investors.

Absolute indicators



Relative indicators



Impact of news and volatility on market activity (synchronous indicators)

$$\widehat{N}^{K}(t) = \alpha_{H}\widehat{H}(t) + \alpha_{Vol}\widehat{Vol}(t) + \epsilon(t)$$

where the new variables are standardized versions of the original ones

Table 3. Summary of the results of the linear regression of equation (8) of the number N^K of trading investors vs. the news intensity signal H and the volatility proxy *Vol*. The number in parentheses is the 5–95% confidence intervals obtained using bootstrap analysis. The last two columns show the results of the partial correlation analysis.

Investor category	α_H	α_{Vol}	% variance of residual of N^K	$\rho(N^K,H Vol)$	$\rho(N^K, Vol H)$
Companies	0.271 (0.205,0.335)	0.517 (0.437,0.597)	51.8	0.309	0.534
Financial	0.195 (0.125,0.264)	0.479 (0.407,0.558)	63.8	0.207	0.461
Governmental	0.238 (0.164,0.303)	0.192 (0.119,0.262)	86.0	0.215	0.180
Non-profit	0.319 (0.249,0.394)	0.270 (0.199,0.344)	73.9	0.305	0.264
Households	0.226 (0.165,0.285)	0.627 (0.554,0.697)	41.4	0.289	0.651
Foreign org.	0.158 (0.094,0.224)	0.442 (0.374,0.517)	70.9	0.160	0.416

Endogenous information drives more the activity of companies, financial, and households investors. The case of governmental and non-profit investors is compatible with the opposite conclusion.

Impact of news and volatility on market activity (overnight indicators)

$$\hat{N}^{K}(t) = \alpha_{H}\hat{H}_{O}(t) + \alpha_{Vol}\hat{V}ol_{O}(t) + \varepsilon(t)$$

Table 6. Summary of the results of the linear regression of equation (8) of the number N^K of trading investors vs. the news intensity signal $H_O(t)$ of overnight news and the overnight volatility proxy $Vol_O(t) = 2 |P_{open}(t) - P_{close}(t-1)|/(P_{open}(t) + P_{close}(t-1))$. The number in parentheses is the 5–95% confidence intervals obtained using bootstrap analysis. The last two columns show the results of the partial correlation analysis.

Investor category	α_{H_O}	α_{Volo}	% variance of residual of N^K	$\rho(N^K,H_O Vol_O)$	$\rho(N^K, Vol_O H_O)$
Companies	0.171 (0.109,0.233)	0.193 (0.142,0.242)	93	0.174	0.195
Financial	0.116 (0.061,0.177)	0.224 (0.163,0.288)	93	0.119	0.225
Governmental	0.133 (0.071,0.195)	0.057 (0.007,0.110)	98	0.133	0.057
Non-profit	0.150 (0.090,0.214)	0.077 (0.021,0.140)	97	0.150	0.078
Households	0.199 (0.130,0.268)	0.262 (0.198,0.333)	88	0.207	0.268
Foreign org.	0.127 (0.066,0.189)	0.195 (0.151,0.245)	94	0.129	0.196

The preeminence of volatility impact is still observed for companies, financial, and households investors but it is much weaker than in the synchronous case. The opposite case of governmental and non-profit investors is in the present case more pronounced.

Impact of news sentiment and return on the unbalance of market activity (absolute indicators)

$$\widehat{\Delta}N_A^K(t) = \alpha_{S_A}\widehat{S}_A(t) + \alpha_{Ret}\widehat{R}et(t) + \epsilon(t)$$

Table 4. Summary of the results of the linear regression of equation (10) of the difference ΔN_A^K between buying and selling investors vs. the absolute sentiment indicator S_A and the stock return *Ret*. The number in parentheses is the 5–95% confidence intervals obtained using bootstrap analysis. The last two columns show the results of the partial correlation analysis.

Investor category	α_{S_A}	α_{Ret}	% variance of residual of ΔN_A^K	$\rho(N_A^K,S_A Ret)$	$\rho(N_A^K, Ret S_A)$
Companies	0.041 (-0.031,0.102)	-0.653 (-0.749,-0.572)	58.0	0.0528	-0.6463
Financial	0.008 (-0.055,0.069)	-0.576(-0.651, -0.516)	66.9	0.0095	-0.5709
Governmental	-0.019(-0.083,0.047)	-0.196(-0.270, -0.125)	95.9	-0.0196	-0.1940
Non-profit	-0.026 (-0.116,0.056)	-0.220(-0.303, -0.136)	94.8	-0.0263	-0.2178
Households	0.060 (-0.012,0.131)	-0.655(-0.745, -0.568)	57.9	0.0781	-0.6474
Foreign org.	-0.006 (-0.072,0.058)	-0.504 (-0.571,-0.438)	74.4	-0.0072	-0.4999

The role of news sentiment is absent within error bars whereas price returns have a large impact. For all investors' categories the unbalance of market activity is anti-correlated with returns (contrarian behavior).

Conclusions

A key aspect of economic and financial systems is that they are heterogeneous open systems processing information.

The knowledge of information is providing marginal advantage and therefore its process of information aggregation is complex.

Tools from statistical and theoretical physics and non conventional data mining approaches are suggesting information filtering procedures that are essential for the understanding of these complex systems.

Trading activity of single investors are affected by both exogenous and endogenous news. Different categories of investors show different reactions to them. Discriminating between exogenous and endogenous news is difficult because the two sets are strongly interlinked.

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Thank you



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- Reality mining
- Price formation, market microstructure
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- Networks in economics and finance
- Agent based models in economics and finance

1 https://sites.google.com/view/varennacs2018/general-information 47